



Note : Attempt (٤) quations only

(Q¹-A) An unconfined compression test has given unconfined compression strength of ١٢٦.٦ kN/m². In CD test the effective shear strength parameters are $c' = ٢٥$ kN/m² and $\phi' = ٣٠^\circ$. If the pore pressure parameter $A = - ٠.٠٩$. Calculate the initial pore pressure in the saturated sample. (١٥ marks)

Solution

$$\begin{aligned}\sigma_{1f}' &= \sigma_{3f}' \tan^2(45 + \phi'/2) + 2c' \tan(45 + \phi'/2) \\ \sigma_{1f}' &= \sigma_{3f}' \tan^2(45 + 30/2) + 2 * 25 \tan(45 + 30/2) \\ \sigma_{1f}' &= 3\sigma_{3f}' + 86.6 \quad \text{--- ①} \\ \text{From unconfined compression test} \\ \sigma_1' - \sigma_3' &= (126.6 - 0) \Rightarrow \sigma_{1f}' = \sigma_{3f}' + 126.6 \quad \text{--- ②} \\ \text{Solving the above equations} \\ \sigma_{3f}' + 126.6 &= 3\sigma_{3f}' + 86.6 \Rightarrow \sigma_{3f}' = 20 \text{ kN/m}^2 \\ \text{In unconfined compression test } \Delta\sigma_3 &\text{ is zero : } u = -20 \text{ kN/m}^2 \\ \text{and } \Delta u &= B [\Delta\sigma_3 + A(\Delta\sigma_1 + \Delta\sigma_3)] \\ \text{for saturated soil } B &= 1 \\ \therefore A &= \frac{\Delta u}{\sigma_1 - \sigma_3} = \frac{\Delta u}{\sigma_{1f}' - \sigma_{3f}'} \\ \therefore -0.09 &= \frac{\Delta u}{126.6} \Rightarrow \Delta u = -11.4 \text{ kN/m}^2 \\ \text{The initial p.w.p is} \\ u_i &= -20 - (-11.4) = \underline{\underline{-8.6 \text{ kN/m}^2}} \quad \text{Ans}\end{aligned}$$

(Q¹-B) drive the equation of the one dimensional consolidation in soil (١٠ marks)

Solution

The first assumption. The continuity equation is

$$k_z \frac{\partial^2 h}{\partial z^2} + k_x \frac{\partial^2 h}{\partial x^2} = \frac{1}{1+e} \left(e \frac{\partial S}{\partial t} + S \frac{\partial e}{\partial t} \right)$$

Where

z: coordinate in the vertical direction



x: coordinate in the horizontal direction

k_x, k_z : coefficient of permeability in x and z-direction

e: void ratio

h: total head

S: degree of saturation

t: time

due to the second assumption $S = 1$ and $\partial S / \partial t = 0$.

for the third assumption

$$k \frac{\partial^2 h}{\partial z^2} = \frac{1}{(1 + e)} \frac{\partial e}{\partial t} \quad \text{Continuity equation ... (١)}$$

$$\sigma_v = \gamma_t z + \text{surface stress} \quad \text{Equilibrium equation ... (٢)}$$

$$\frac{\partial e}{\partial \bar{\sigma}_v} = -a_v \quad \text{Stress - strain (٣)}$$

Where a_v is coefficient of compressibility

Breaking the total head into its components

$$h = h_e + \frac{u}{\gamma_w} = h_e + \frac{1}{\gamma_w} (u_{ss} + u_e)$$

Where: h_e : elevation head

u_{ss} : steady state pore pressure

u_e : excess pore pressure

we have

$$\frac{\partial^2 h_e}{\partial z^2} = 0 \quad \frac{\partial^2 u_{ss}}{\partial z^2} = 0$$

so

$$\frac{k(1 + e)}{\gamma_w a_v} \frac{\partial^2 u_e}{\partial z^2} = - \frac{\partial \bar{\sigma}_v}{\partial t}$$



if

$$c_v = \frac{k(1 + e)}{\gamma_w a_v} = \frac{k}{\gamma_w m_v}$$

where m_v : is the coefficient of volume change

c_v : coefficient of consolidation

$$c_v \frac{\partial^2 u_e}{\partial z^2} = \frac{\partial u_e}{\partial t} - \frac{\partial \sigma_v}{\partial t}$$

If total stress is constant with time $\frac{\partial \sigma_v}{\partial t} = 0$

The initial excess pore pressure is uniform with depth

There is a drainage at both top and bottom of the consolidation stratum

Let H_{dr} is length of maximum drainage bath and $T = \frac{c_v t}{H^2}$ where T is time factor

$$\frac{\partial^2 u_e}{\partial Z^2} = \frac{\partial u_e}{\partial T} \quad \text{Solving this equation satisfying the following condition}$$

Initial condition at $t = 0$, $u_e = u_0$ for $0 \leq z \leq H$, u_0 = initial $\frac{z}{H_{dr}}$ excess p.w.p

Boundary condition at all t

$u_e = 0$ for $\frac{z}{H_{dr}} = 0$ and H , the solution of this equation is

$$u_e = \sum_{m=0}^{m=\infty} \frac{2u_0}{M} (\sin MZ) e^{-M^2 T} \quad \text{where} \quad M = \frac{\pi}{2} (2m + 1)$$

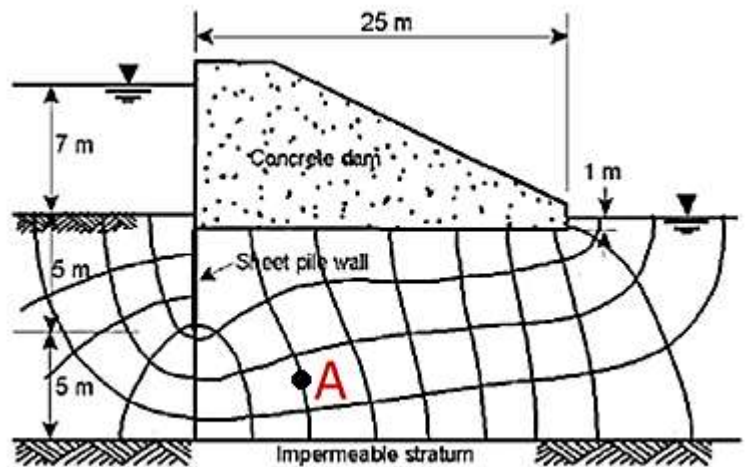
m : is dummy variable taking on values ١, ٢, ٣, ٤

The solution is conveniently portrayed in the graph (Isochrones) as shown

$$U_z = 1 - \frac{u_e}{u_0}$$



(Q٢-A) The concrete dam ٢٥ m long shown in Figure is embedded ١ m into the ground surface and has a sheet pile wall ٥ m deep at its heel. The headwater is ٧ m deep and the tail water is at ground surface. The permeability of the soil is $k=٢ \times ١٠^{-٤}$ cm/sec both vertically and horizontally. Calculate the seepage under the dam and the Pore Water pressure at A; A is ٢m above the impervious layer.



(١٢ marks)

Solution

$$h = 7 \text{ m}, N_f = 4, N_d = 13, H = 10$$

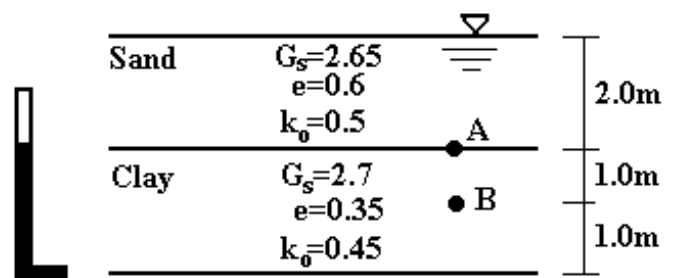
$$\text{Pressure head per net} = 7/13 = 0.54$$

$$\text{Pressure head at A} = h + H - (\text{No. of potential at A} \times \text{Pressure head per net}) - z$$

$$= 7 + 10 - (6.5 \times 0.54) - 2 = 11.49 \text{ m}$$

$$\text{Pore Water pressure at A} = 11.49 \times 9.81 = \underline{112.717 \text{ kN/m}^2}$$

(Q٢-B) Compute the vertical and horizontal effective and total stresses at A and B for the profile shown (١٢ marks)





3 Let $k_{sand} = k_{clay}$

$$f_{soil sand} = f_{soil clay}$$

$$k_{i sand} = k_{i clay}$$

$$\frac{\Delta h}{l_{sand}} = \frac{\Delta h}{l_{clay}} \Rightarrow \frac{4 - h_{tA}}{2} = \frac{h_{tA} - 2}{2}$$

$$2h_{tA} = 6 \therefore h_{tA} = 3 \text{ m}$$

$$h_{pA} = 3 - 2 = 1 \text{ m}$$

$$h_{pB} = 2.5 - 1 = 1.5 \text{ m}$$

$$\gamma_{t sand} = \frac{G + Se}{1 + e} \gamma_w = \frac{2.65 + 0.6}{1 + 0.6} \times 9.81 = 19.927 \text{ kN/m}^3$$

$$\gamma_{sat clay} = \frac{2.7 + 0.35}{1 + 0.35} \times 9.81 = 22.163 \text{ kN/m}^3$$

$$\sigma_{VA} = 19.927 \times 2 = 39.854 \text{ kN/m}^2 \quad \sigma'_{VA} = 39.854 - 9.81 = 30.044 \text{ kN/m}^2$$

$$\sigma'_{hA} = 30.044 \times 0.5 = 15.022 \text{ kN/m}^2 \quad \sigma_{hA} = 15.022 + 9.81 = 24.832 \text{ kN/m}^2$$

$$\sigma_{VB} = 39.854 + 1 \times 22.163 = 62.017 \text{ kN/m}^2$$

$$\sigma'_{VB} = 62.017 - 1.5 \times 9.81 = 47.302 \text{ kN/m}^2$$

$$\sigma'_{hB} = 47.302 \times 0.45 = 21.286 \text{ kN/m}^2$$

$$\sigma_{hB} = 21.286 + 1.5 \times 9.81 = 36.009 \text{ kN/m}^2$$

(Q2-A) A direct shear box test was conducted on a sample of sand, gave the following observations at the time of failure, normal stress = $\lambda \cdot \text{kN/m}^2$; shear stress = $\epsilon \lambda \text{ kN/m}^2$. Determine:

- the angle of internal friction;
- the magnitude and direction of principle stress in the zone of failure;
- the magnitude of maximum deviator stress if a sample of the same sand with the same void ratio were tested in the UU test with an all round pressure of 0.8 kN/m^2 .

(10 marks)

Solution



$$\begin{aligned}
 (a) \quad \phi &= \tan^{-1}\left(\frac{c}{\sigma_h}\right) = \tan^{-1}\left(\frac{48}{80}\right) = \underline{31^\circ} \\
 (b) \quad \theta &= 45 + \phi/2 = 45 + \frac{31}{2} = \underline{60.5^\circ} \\
 \sigma_h &= \frac{\sigma_1 + \sigma_3}{2} + \frac{\sigma_1 - \sigma_3}{2} \cos(121) \\
 80 &= \frac{\sigma_1 + \sigma_3}{2} + \frac{\sigma_1 - \sigma_3}{2} (-0.515) \quad \text{--- (1)} \\
 c &= \frac{\sigma_1 - \sigma_3}{2} \sin 2\theta \Rightarrow 48 = \frac{\sigma_1 - \sigma_3}{2} (0.857) \\
 \therefore 80 &= \frac{112 + \sigma_3 + \sigma_3}{2} + \frac{112 + \sigma_3 - \sigma_3}{2} (-0.515) \\
 80 &= 56 + \sigma_3 - 28.84 \\
 \therefore \sigma_3 &= \underline{52.8 \text{ kN/m}^2} \\
 \sigma_1 &= 112 + 52.84 = \underline{164.84 \text{ kN/m}^2} \\
 (c) \quad \sigma_1 &= \sigma_3 \left(\frac{1 + \sin \phi}{1 - \sin \phi} \right) \\
 \sigma_1 &= \sigma_3 \left[\frac{1 + \sin 31}{1 - \sin 31} \right] = 58 \times 3.124 = 181.19 \text{ kN/m}^2 \\
 \therefore \sigma_d &= \sigma_1 - \sigma_3 = \underline{123.194 \text{ kN/m}^2}
 \end{aligned}$$

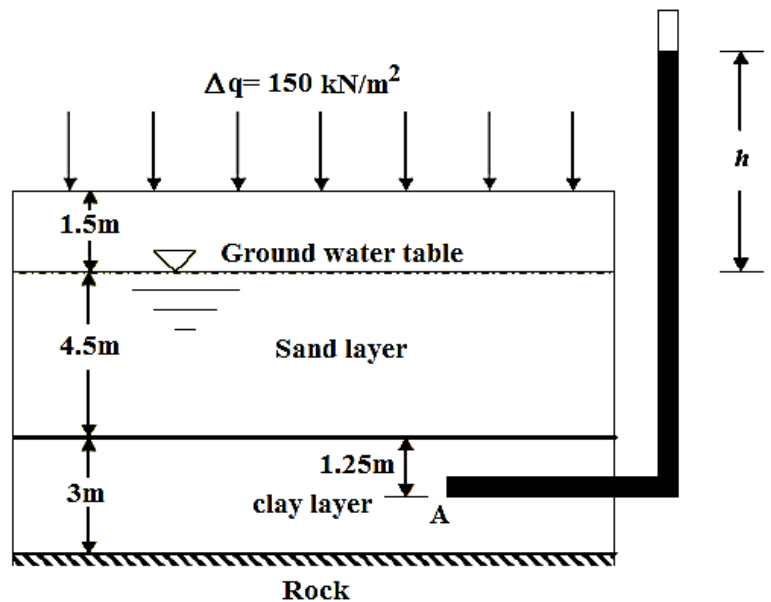
(Q٢-B) Dry soil with $G_s = 2.7$ is mixed with ١٦% by weight of water and compacted to produce a cylinder samples of ٣٨ mm diameter and ٧٦ mm long with ٦% air content. Calculate the mass of the mixed soil that will be required and the void ratio of the sample. (١٠ marks)

$$\begin{aligned}
 V &= 7.6 \times \frac{\pi (3.8)^2}{4} = 86.19 \text{ cm}^3 \quad \gamma_s = G_s \gamma_w = 2.71 \times 9.81 = 26.585 \text{ kN/m}^3 \\
 V_s &= V_w + V_a = 86.19 \text{ cm}^3 = 8.619 \times 10^{-5} \text{ m}^3 \\
 \frac{W_s}{26.585} + \frac{0.16 W_s}{9.81} + 0.06 \times 8.619 \times 10^{-5} &= 8.619 \times 10^{-5} \\
 \therefore W_s &= 0.0015014 \text{ kN} \\
 W_s &= V_s \times \gamma_s = V_s \times G_s \times \gamma_w \\
 0.0015014 &= V_s \times 2.71 \times 9.81 \\
 \therefore V_s &= 5.648 \times 10^{-5} \text{ m}^3 \\
 V_v &= V - V_s = 8.619 \times 10^{-5} - 5.648 \times 10^{-5} \\
 &= 2.971 \times 10^{-5} \\
 e &= V_v / V_s = \frac{2.971 \times 10^{-5}}{5.648 \times 10^{-5}} = 0.526
 \end{aligned}$$

(Q4-A) For the profile shown :

- (a) How high (h) will the water rise in the piezometer immediately after the application of the surface load of 100 kN/m².

- (b) Find the increment of effective stress in point (A) due to application of 100 kN/m² after 4 months, $c_v = 1.68 \times 10^{-4}$ cm²/sec



(10 marks)

Solution



- (a) The height in piezometer is
(١٥٠/٩.٨١) - ٤.٥ - ١.٢٥ = ٩.٥٤m
- (b)

$$T = \frac{C_v t}{H^2}, \quad C_v = 8.68 \times 10^{-4} \text{ cm}^2/\text{sec}$$

$$L = 4 \times 30 \times 60 \times 60 = 10368000 \text{ sec}$$

$$H = 1.25 \times 100 = 125 \text{ cm}$$

$$T = \frac{8.68 \times 10^{-4} \times 10368000}{(125)^2} = 0.576$$

$$\frac{z}{H_{dr}} = \frac{1.25}{3} = 0.4167$$

From chart $U = 0.78$

increase in stress $= 150 \times (1 - 0.78) = 33 \text{ kN/m}^2$

(Q4-B) Defined: liquid limit, pressure head, consistency, Residual soils, equipotential lines (10 marks)

liquid limit: is the moisture content in percent at which the soil changes from liquid to plastic state

Pressure head: is the height of the vertical column of water in the piezometer installed at that point

Consistency: Soil consistency is the strength with which soil materials are held together or the resistance of soils to deformation and rupture.. Soil consistency may be estimated in the field using simple tests or may be measured more accurately in the laboratory.

Residual soils: the soils formed by the weathered products at their place of origin

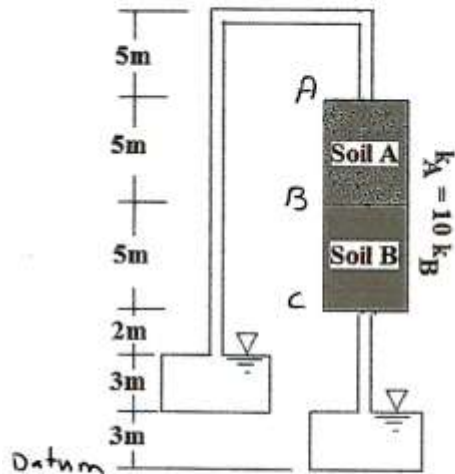
Equipotential lines: is a line along which the potential (total) head at all points is the same

(Q5-A) For the setup shown, Find total head (h_t), Elevation head (h_e) and Pressure head (h_p) for the soil the setup shown



(١٥ marks)

Solution



$$Q_A = Q_B$$

$$k_A i_A = k_B i_B$$

$$k_A \times \frac{\Delta h_A}{L_A} = k_B \times \frac{\Delta h_B}{L_B}$$

$$10 k_B \Delta h_B = k_B \Delta h_B$$

$$10 \times (6 - h_{tB}) = (h_{tB} - 3)$$

$$-10h_{tB} + 60 = h_{tB} - 3$$

$$11h_{tB} = 63 \therefore h_{tB} = 5.73 \text{ m}$$

	h_e	h_p	h_t
A	18	-12	+6
C	8	-5	+3
B	13	-7.27	5.73

- (Q^o-B) A soil element is subjected to an initial stresses $P_o = 400 \text{ kN/m}^2$ and $q = 0$. Compute the value of σ_h at $\sigma_v = 600 \text{ kN/m}^2$ for the following:
- (A) If the stresses increased such that $\Delta\sigma_v = 3\Delta\sigma_h$
- (B) $\Delta\sigma_v = 0$ (10 Marks)



$$T = \frac{c_v t}{H^2}, \quad c_v = 8.68 \times 10^{-4} \text{ cm}^2/\text{sec}$$

$$t = 4 \times 30 \times 60 \times 60 = 1036800 \text{ sec}$$

$$H = 1.25 \times 100 = 125 \text{ cm}$$

$$T = \frac{8.68 \times 10^{-4} \times 1036800}{(125)^2} = 0.576$$

$$\frac{z}{H_{dr}} = \frac{1.25}{3} = 0.4167$$

From chart $U = 0.78$

increment in stress $= 150 \times (1 - 0.78) = 33 \text{ kN/m}^2$

(A) $\Delta p = \frac{\Delta \sigma_v + \Delta \sigma_h}{2} = \frac{3\Delta \sigma_h + \Delta \sigma_h}{2} = 2\Delta \sigma_h$

$$\Delta q = \frac{\Delta \sigma_v - \Delta \sigma_h}{2} = \frac{3\Delta \sigma_h - \Delta \sigma_h}{2} = \Delta \sigma_h$$

$$\therefore \frac{\Delta q}{\Delta p} = \frac{1}{2}$$

$$\frac{q - 0}{p - 400} = \frac{1}{2} \Rightarrow q = 0.5p - 200$$

$$\therefore \frac{600 - \sigma_h}{2} = 0.5 \frac{600 - \sigma_h}{2} - 200$$

$$\therefore \sigma_h = 1350$$

(B) $\Delta \sigma_v = 0$

$$\Delta p = \frac{0 + \Delta \sigma_h}{2}, \quad \Delta q = \frac{0 - \Delta \sigma_h}{2}$$

$$\frac{\Delta q}{\Delta p} = -1$$

$$\therefore \Delta q = -\Delta p$$

$$\frac{600 - \sigma_h}{2} = -\frac{600 - \sigma_h}{2}$$

$$300 - \frac{\Delta \sigma_h}{2} = -300 + \frac{\Delta \sigma_h}{2}$$

$$\sigma_h = \infty$$